

# Vertical cracking of reinforced concrete cylindrical tank wall at early age state

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**ABSTRACT:** Ten cylindrical reinforced concrete tanks realized last year in Cracow are subject of this paper. Due to the construction and technology solution which has been applied it was necessary to realize construction joints in vertical and horizontal direction as well as two expansion joints. In spite of such solution, many vertical cracks on some wall segments under construction have been found. Based on the preliminary analysis it was stated the reasons of early age concrete cracking.

## 1 STRUCTURE UNDER INVESTIGATION AND CONCRETE PROPERTIES

Nowadays in Cracow there is realized the greatest sewage-treatment plant in Poland. Ten cylindrical reinforced concrete tanks in monolithic technology were constructed in 2004. The authors of this paper have had possibility to observe the methods of execution these tanks as well as to check up the development of mechanical concrete properties at early age.

The concrete class C25 has been used to construction the floor slab, the cylindrical footing and the wall all of the cylindrical tanks. The metallurgical cement CEM III/A-32,5N type and the Portland rapid-hardening cement with slag addition CEM II/B-S-32,5R type have been applied as equivalent.

The wall of the cylindrical tank no 4 under investigation, has been constructed of concrete based on cement CEM II/B-S-32,5R type. Development of concrete strength is presented in Table 1.

Table 1. Development of concrete strength.

Age of concrete [days]	Compressive strength [MPa]		Tensile strength [MPa]	
	15x15x15	15x30	by splitting 15x15x15	in direct tension 15x30
1	5.27	-	0.59	-
2	13.60	-	1.31	-
3	17.11	14.87	1.54	1.40
7	25.22	20.71	1.99	1.70
14	29.78	-	2.25	-
28	35.88	30.41	2.64	2.01
90	50.44	43.92	4.02	2.60

The cylindrical wall has been concreted in segmental system of the height equal to 5.5 m. Whole circumference has been divided in 10 segments. All con-

struction joints were fully waterstopped using conventional PVC material. The cross section of the tank wall and the location of construction joints are presented in Figure 1.

Reinforcing chairs were used in all walls and slabs to insure that the specified 50 mm cover was maintained consistently. The hydraulic curing methods such as wet burlap and sprinkling have been applied for crack control and curing.

In the first stage every second wall segment has been constructed starting from segments 2 and 10 (30.06). Afterwards the segments 8 and 6 (3.07), segment 5 (6.07), 3 and 1 (8.07), 9 and 7 (10.07), 5a (14.07) and segment 4 (15.07) have been concreted. The day before closing of the tank wall circumference it has been found vertical cracking almost in each segment. Location of principal cracks measured at the height equal to 0.7m in relation to the floor slab is shown in Figure 1. Some of them are through at the wall thickness. Location of the cracks on the inside and outside surfaces of the wall segments 8 and 9 are presented in Figure 3 and 4 respectively.

Compressive strength was monitored closely during construction, since higher than required strength would lead to excessive heat generation during hydration, and thus to shrinkage cracking. An excellent coefficient of variation in compressive strength was observed during the majority of concrete production. Air entrainment was also closely monitored because of its importance to concrete permeability and longterm corrosion resistance. The tanks no 1 and 2 were hydrostatically tested by slowly filling with subsoil water. The tank under discussion will be tested this year.

## 2 THERMAL CRACKING

Lokhorst & Breugel (1995) have analyzed the problem of thermal cracking in a wall and in a wall-slab structure. The self-equilibrating stresses in the wall increased with: decreasing ambient temperatures, increasing wall thickness, early removal of formwork, reactivity of the cement, increasing wind velocity.

Additional stresses will develop if a part of the average load-independent axial deformations of the wall is restrained.

For a degree of restraint of 0% the structure is free to bend and to deform in axial direction. At 100% restraint the both bending and axial deformations are prevented completely. Walls thicker than 0.5m were likely to crack in most cases. In thin walls wind may have a positive effect since it reduces the peak temperatures and the temperature differentials between wall and slab. The probability of cracking increased for higher initial temperatures of the concrete mix.

The development of the average concrete temperature in the cross section of the wall and the ambient temperature are presented in Figure 2. Seasonal temperatures taken from meteorological office in Cracow ranged from 8.0°C to 30.8°C in the period from 30.06 to 30.07.2004.

The real temperatures values measured at building place were higher. The calculations of average concrete temperature in the cross section have been done taking into consideration the initial temperatures of the concrete mixture measured in each day of concreting: 30.06 (25.07°C), 3.07 (23.1°C), 6.07.2004 (23.1°C), 8.07 (30.1°C), 10.07 (26.4°C) and 15.07 (22.75°C). The maximal and minimal values of average concrete temperatures for each wall segment are shown in Figure 2.

## 3 DEVELOPMENT OF THE TEMPERATURE IN THE HARDENING CONCRETE

The calculation of the mean temperature variation in hardening concrete has been done based on (Kiernożycki, 2003). The thermal material properties used in the temperature calculation are:  $\lambda_b$  - 2.59W/Mk, the thermal conductivity was calculated on the basis of concrete composition (Kiernożycki, 2003), however with respect to calculation which was made during the first week of hardening concrete, the value of thermal conductivity was increased by 20% (Rostasy, 2001) up to value 3.11W/mK.

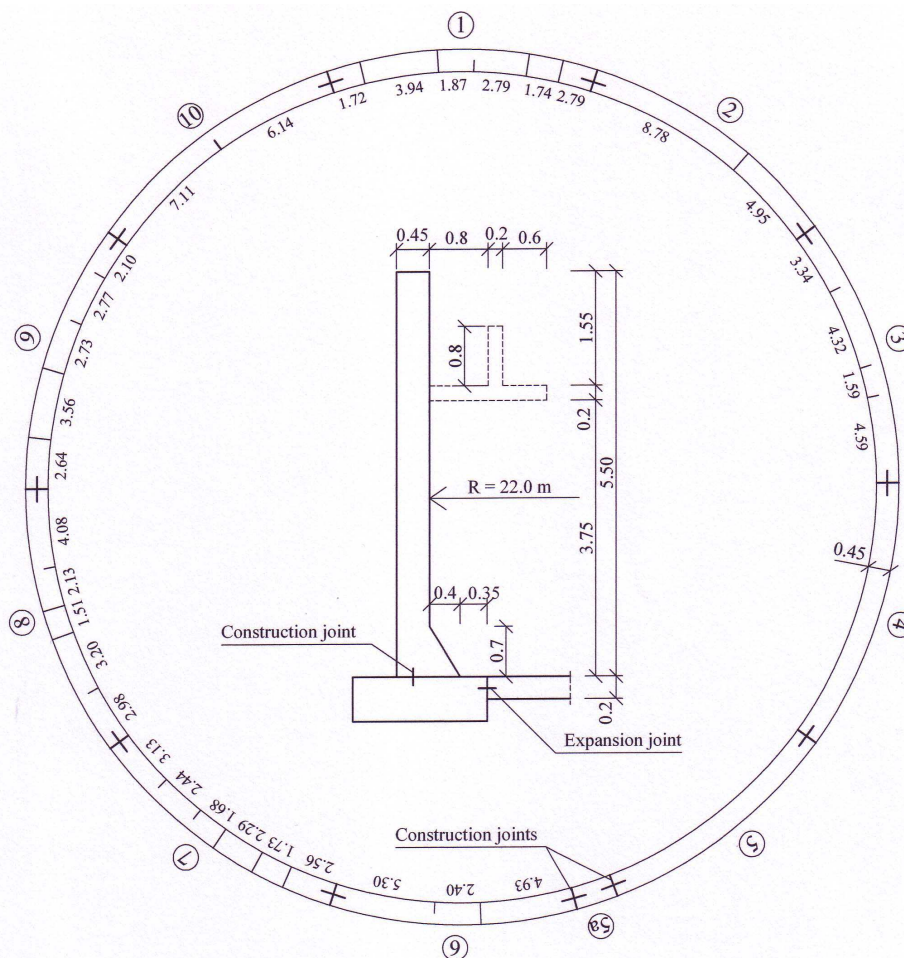


Figure 1. Cylindrical reinforced concrete tank geometry and construction joints layout.

$c_b = 0.772 \text{ kJ/kgK}$ , the coefficient of heat capacity also was calculated based on the concrete composition.

$\alpha = 5.8 \text{ W/m}^2\text{K}$ , the convection coefficient was assumed according to Townsend (1959) under the assumption that the value of wind speed is equal to zero. In case of the wall in the formwork it has been assumed the substitute convection coefficient  $\alpha_w$  expressed as follows:

$$\alpha_w = \frac{\alpha}{R\alpha + 1} \quad \text{and} \quad R = \frac{d}{\lambda}$$

where:  $d$  = the thickness of the formwork,  $\lambda$  = the thermal conductivity of the formwork.

The solution of the heat transport equation (2) in case of one-way heat transport with the assumption that a function  $Q$  is described by (3), is given by K. Hirschfeld (1948). Based on the assumption that the heat transfer on the both surfaces of concrete wall is the same, the mean temperature in a cross section of the wall can be written as follows:

$$\bar{T}(t) = \left[ \frac{2\alpha(1-k) + dc_b\gamma_b K_{Tp}}{2\alpha k - dc_b\gamma_b K_{Tp}} \right] \cdot \frac{qC}{c_b\gamma_b} \exp(-K_{Tp}t) + \dots$$

$$\left[ T_p - T_o - \frac{qCdK_{Tp}}{2\alpha_o^n - dK_{Tp}c_b\gamma_b} \right] \dots$$

$$f(\varphi_1) \exp\left(-\frac{\alpha_o}{c_b\gamma_b d}t\right) + T_o \quad (1)$$

$$\frac{\partial T}{\partial \tau} = a_b \cdot \nabla^2 T + \frac{\partial Q}{\partial \tau} \cdot \frac{1}{c_b \cdot \gamma_b} \quad (2)$$

$$Q(\tau) = C \cdot q \cdot [1 - \exp(-K_{Tp} \cdot t)] \quad (3)$$

where:  $\varphi_1$  = is the solution of:  $\varphi_1 \text{tg} \varphi_1 = \frac{\alpha d}{2\lambda} = B_i$ ,

$$P = \frac{d^2 K_{Tp}}{4a_b} - \text{Predwoditielew's number,}$$

$$f(\varphi_1) = \frac{2 \sin^2 \varphi_1}{\varphi_1^2 \left(1 + \frac{\sin 2\varphi_1}{2\varphi_1}\right)}, \quad \alpha_o^n = \frac{2\lambda\varphi_1^2}{d}$$

$k = \text{ctg} \sqrt{P} \cdot \sqrt{P}$ ,  $T_o$  – temperature of atmospheric air,  $T_p$  – initial temperature of concrete.

The influence of the ambient temperature on the mean temperature in the wall has been taken into account by calculating changes in time of relative difference temperatures value (mean on the whole cross section) depending on Fourier's number (Bogusłowski 1975).

The solution of the temperature development in hardening concrete presented above, is only an approximation of the real temperature in the cross

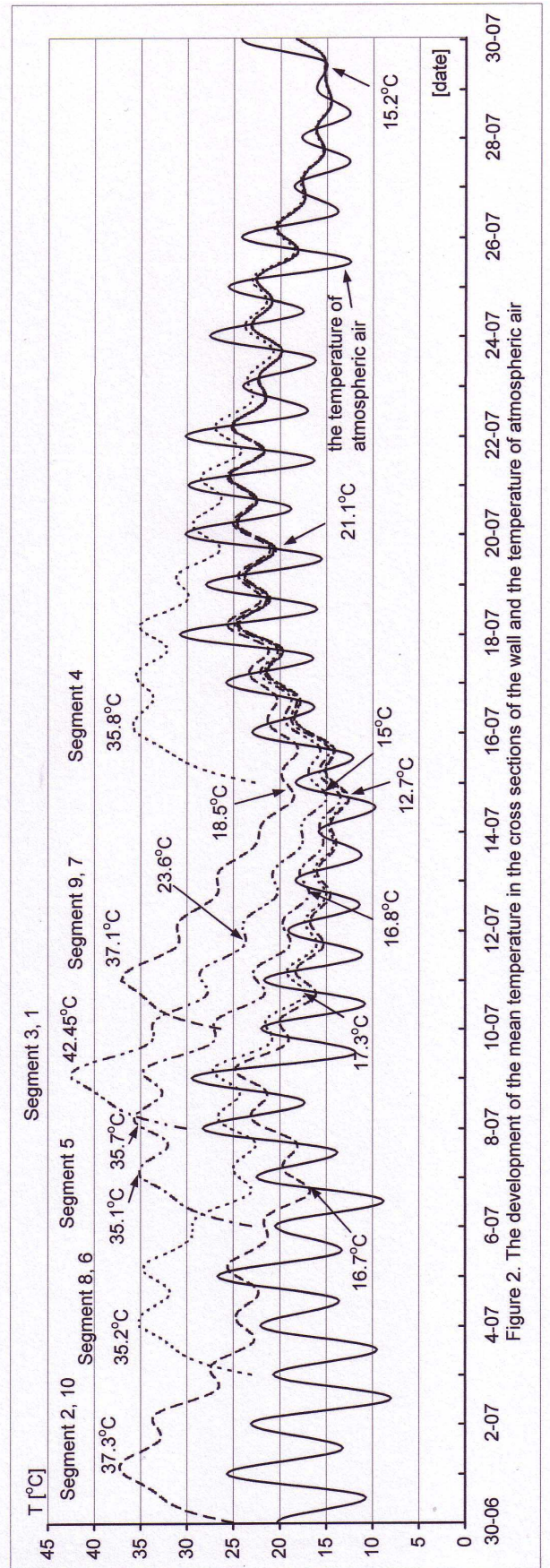


Figure 2. The development of the mean temperature in the cross sections of the wall and the temperature of atmospheric air

section, because it has not been taken into account the effect of the solar radiation and the distribution of the temperature in the cross section. Moreover, in the calculation it has not been taken into account the influence of the moisture on the temperature. In the further works these phenomena will be taken into the analysis.

## 4 FINAL CONCLUSION

Localization and layout of vertical cracks along the height of the wall segment 8 and 9 are presented in Figures 3 and 4 respectively. As it is shown the cracks width ranged from 0.05 to 0.30 mm. In the

wall segments constructed in the second stage there are more cracks and they are uniform distributed. In the segment walls constructed in the first stage there are less cracks and they are located in the middle part of the segment. The displacement of the wall segment is restrained only by floor slab. Later,

when the cylindrical tank wall is closed and the average temperature in the wall is stabilized the existing cracks are developed. The new cracks are formed very rarely.

Temperature differences between maximal and minimal values for wall segments 2 and 10, segment 8 and 6, segment 5, segment 3 and 1, segment 9 and 7 are equal to: 20.6°C; 22.5°C; 23.0°C; 27.45°C and 18.6°C respectively.

In case of the wall segment 5 there are not cracks in spite of temperature difference equal to 23.0°C. It can be explained by increasing the ambient temperature for several days from the time of its construction.

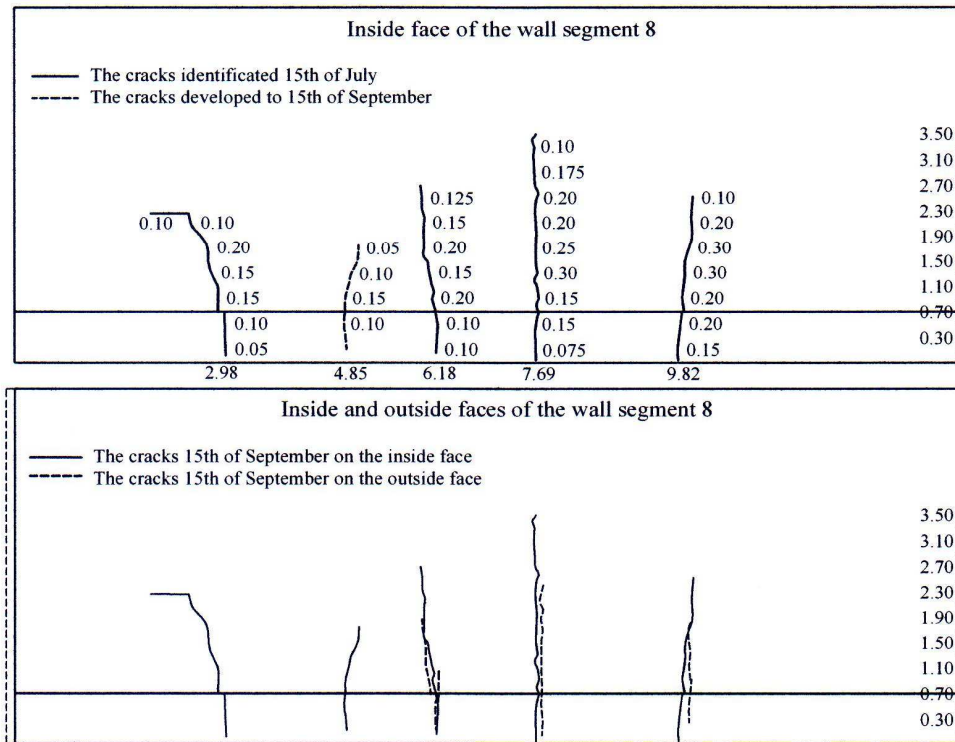


Figure 3. Location of the vertical cracks along the height of the wall segment 8.

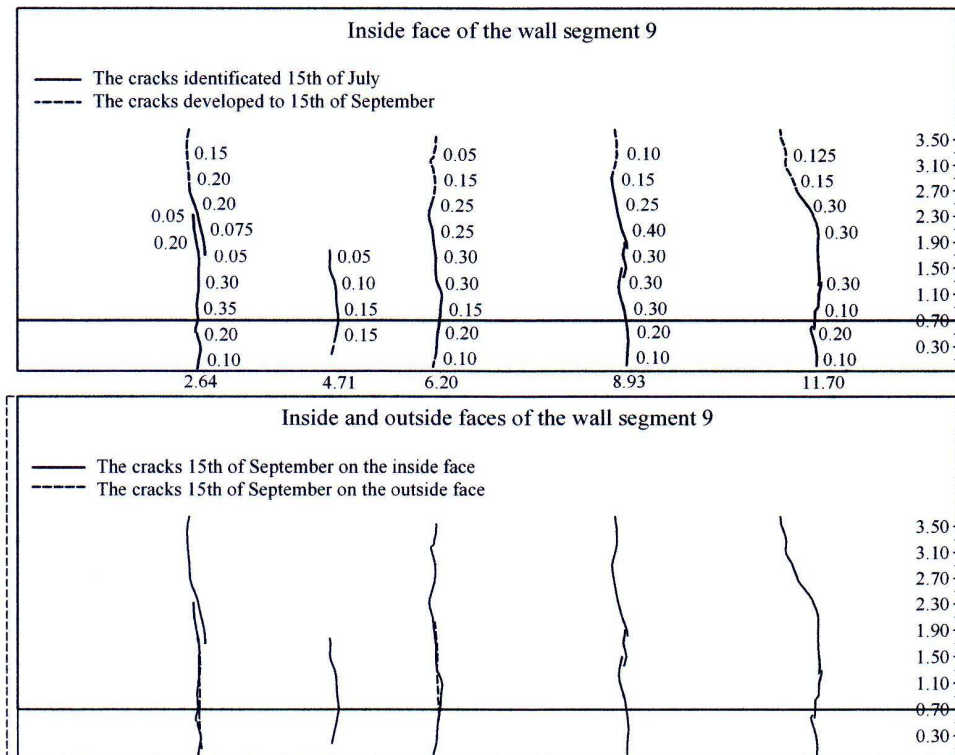


Figure 4. Location of the vertical cracks along the height of the wall segment 9.

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